



Arguing with quantifiers

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Helen of Troy



Dante Gabriel Rossetti (1828–1882)

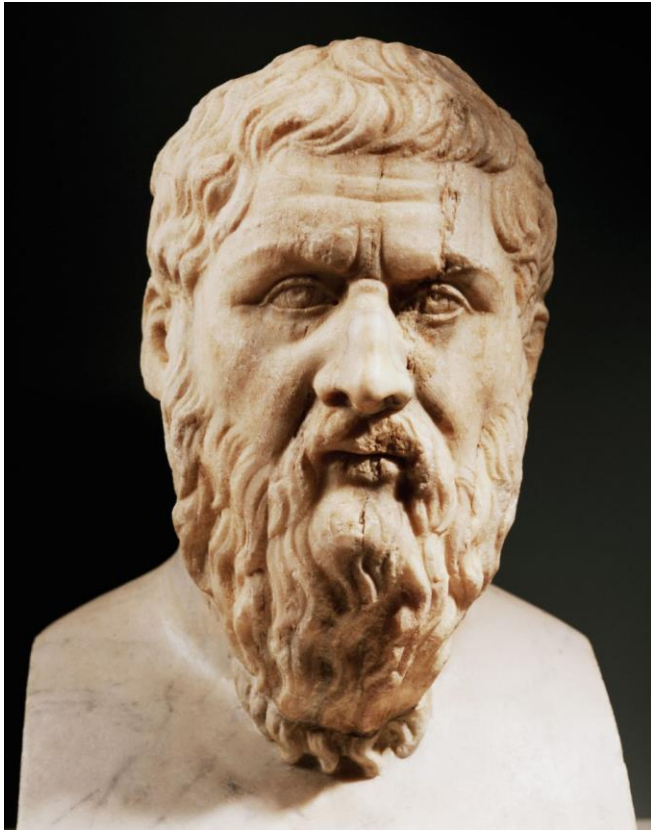
Some say a host of horsemen, others of infantry and others
of ships, is the most beautiful thing on the dark earth
but I say, it is what you love

Full easy it is to make this understood of one and all: for
she that far surpassed all mortals in beauty, Helen her
most noble husband

Deserted, and went sailing to Troy, with never a thought for
her daughter and dear parents.

— Sappho, fragment 16

Gorgia's *Encomium of Helen*



Gorgias (483–375 BC)

- by the gods
- by physical force
- by love
- by speech

“Speech is a powerful master and achieves the most divine feats with the smallest and least evident body. It can stop fear, relieve pain, create joy, and increase pity”

(Gorgias 31)

Argument and quantities

- They are offering at most 50% off last season's stock.
- They are offering up to 50% off last season's stock.

Background story

Imagine you have been hired as a marketing consultant for Green Valley High School. Part of your job is to write a report on the results of standardized math exam questions. These results have been published for Green Valley and for your main rival, Riverside High School.

It's important that you don't tell any lies in the report, but you don't have to report objectively on the facts. **Your aim is to make Green Valley sound like a school whose students have a high probability of success on the exam questions, and Riverside sound like a school whose students have a low probability of success.**

Arguing with quantifiers

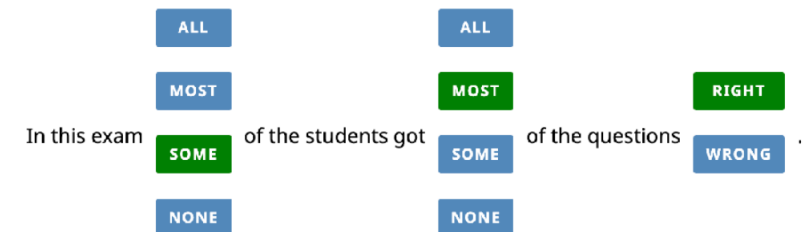
Lesly
Alex
Lisa
Jan
Daniel

Experimental design

- N=60 (via Prolific)
- Stimulus: answers array
 - 0, 3, 9, and 12 right answers possible
 - In decreasing order in array
- Task: Complete sentence frame
 - ‘Q1 of the students got Q2 of the questions ADJ’
 - Q: {none, some, most, all}
 - ADJ: {right, wrong}
 - 32 possible utterances
- Two conditions: high vs low framing
 - Within-subjects
- Each participant saw all 20 situations
 - 10 in high cond, 10 in low cond

Describe these results of **Green Valley** so as to make it appear as if there is a **high** success rate without lying.

Lisanne	✓	✓	✓	✓	✓	✓	✓	✓	✓	✗	✗	✗
Mia	✓	✓	✓	✓	✓	✓	✓	✓	✓	✗	✗	✗
Julia	✓	✓	✓	✗	✗	✗	✗	✗	✗	✗	✗	✗
Theresa	✓	✓	✓	✗	✗	✗	✗	✗	✗	✗	✗	✗
Julian	✓	✓	✓	✗	✗	✗	✗	✗	✗	✗	✗	✗



Raw data

Positive condition

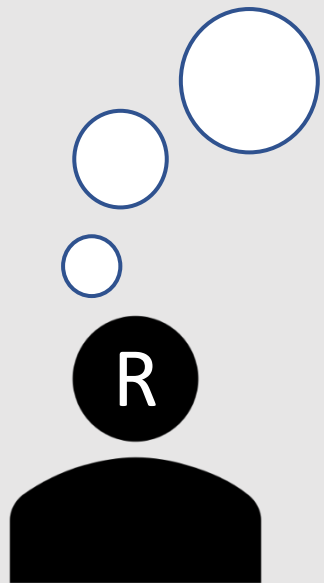
response	obs
<u>some some right</u>	<u>3 3 0 0 0</u>
all some right	3 3 3 3 3
most some right	9 9 3 0 0
some all right	12 12 0 0 0
<u>some all right</u>	<u>12 12 9 0 0</u>
most all right	12 12 12 0 0
most most right	12 12 9 3 3
most all right	12 12 12 3 3
<u>most all right</u>	<u>12 12 12 9 9</u>
all all right	12 12 12 12 12

Raw data

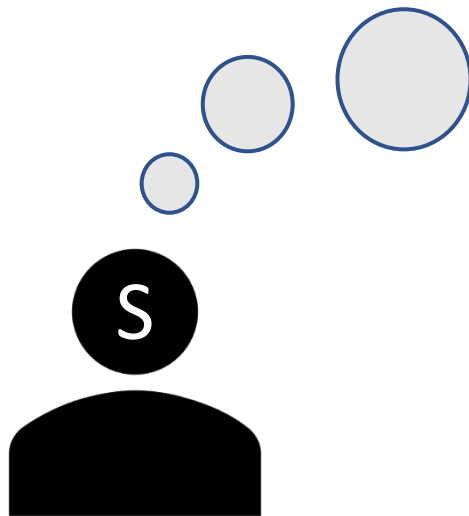
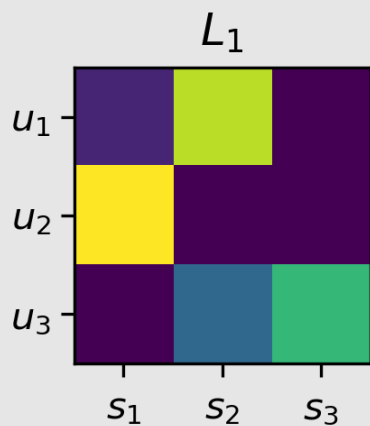
Theresa	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓
Nico	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓
Julian	✓	✓	✓	✗	✗	✗	✗	✗	✗	✗	✗	✗
Susanne	✓	✓	✓	✗	✗	✗	✗	✗	✗	✗	✗	✗
Johann	✓	✓	✓	✗	✗	✗	✗	✗	✗	✗	✗	✗

Tim	✓	✓	✓	✗	✗	✗	✗	✗	✗	✗	✗	✗
Tina	✓	✓	✓	✗	✗	✗	✗	✗	✗	✗	✗	✗
Chris	✗	✗	✗	✗	✗	✗	✗	✗	✗	✗	✗	✗
Lisa	✗	✗	✗	✗	✗	✗	✗	✗	✗	✗	✗	✗
Thomas	✗	✗	✗	✗	✗	✗	✗	✗	✗	✗	✗	✗

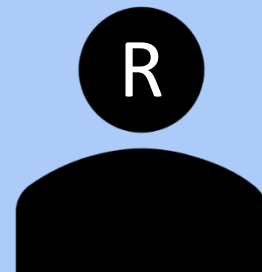
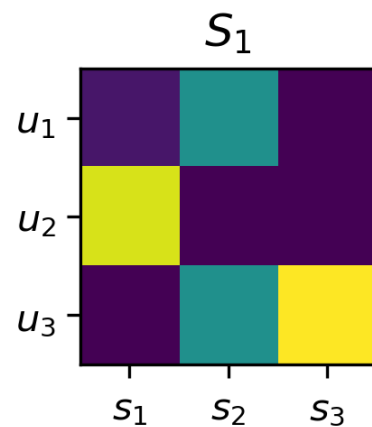
- High condition:
 - 22 'some | all | right'
 - 2 'most | some | right'
- Low condition:
 - 16 'most | most | wrong'
 - 7 'some | most | wrong'
- High condition:
 - 24 'some | some | right'
 - 1 'none | none | wrong' (=all | some | wrong)
- Low condition:
 - 16 'most | all | wrong'
 - 6 'all | most | wrong'



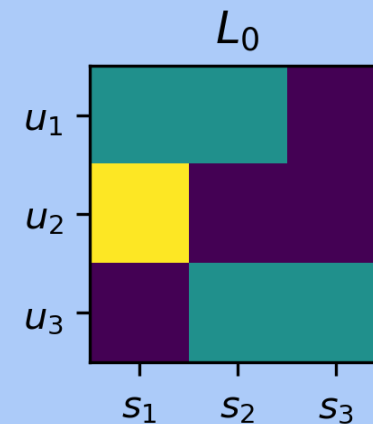
Gets a signal,
does Bayesian
updating



Sees a state, tends to
send the message
most useful to S



Gets a signal,
guesses uniformly
among the
compatible states.



Extending the RSA model

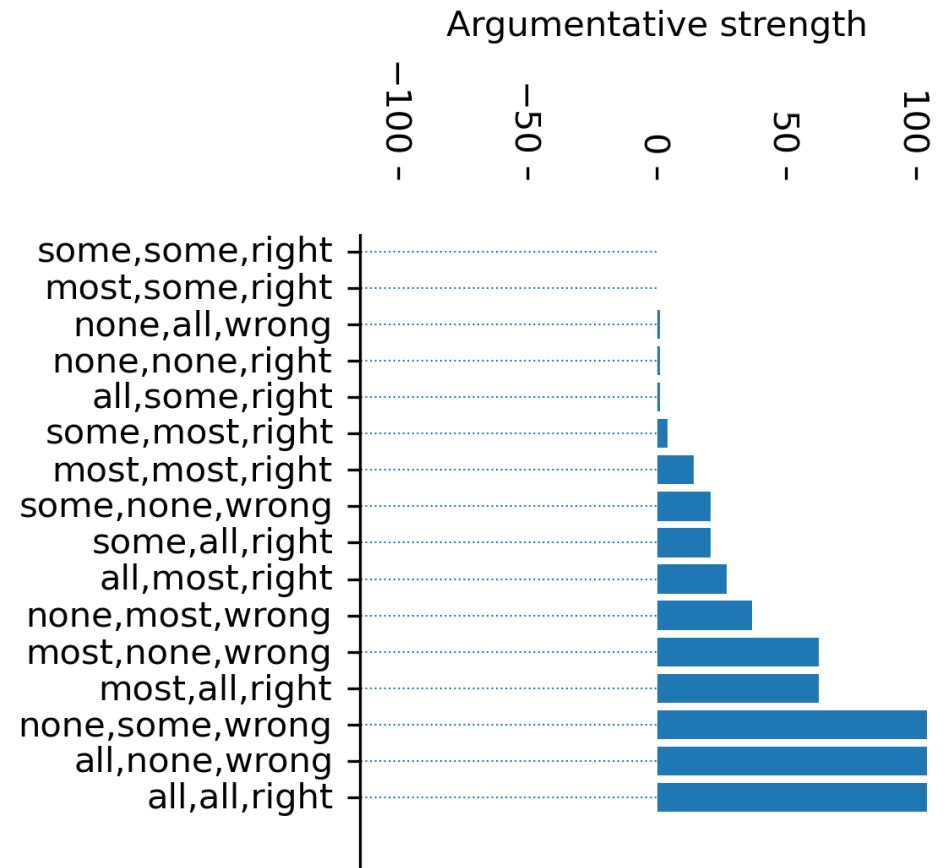
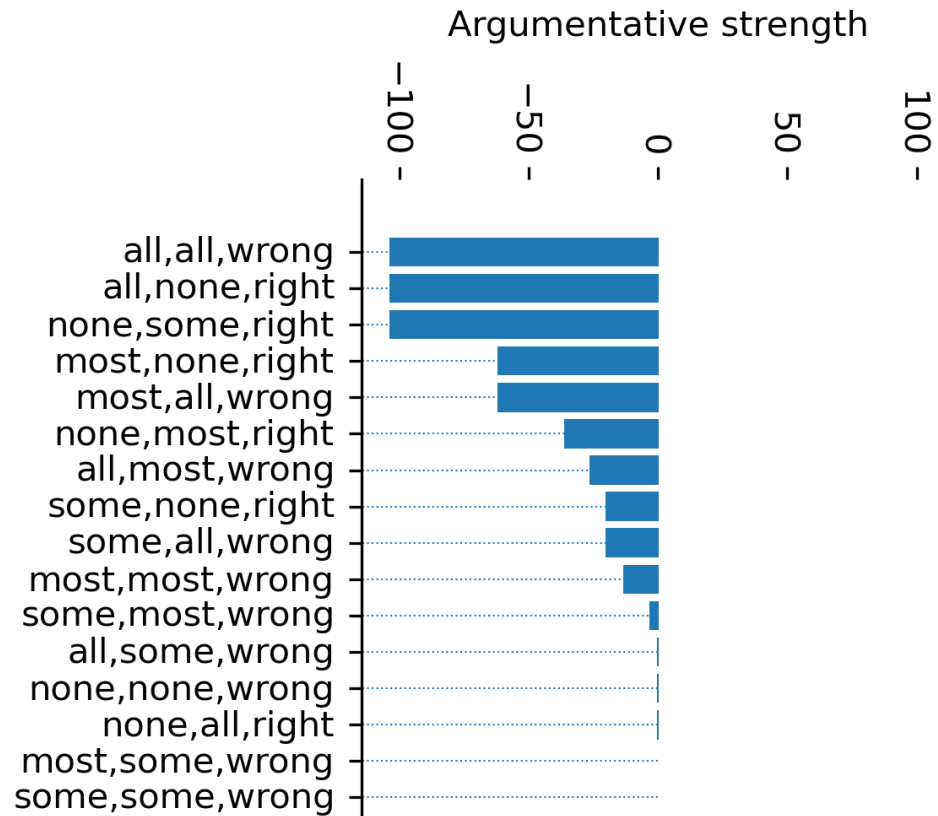
$$\text{Util}(s, u) = \log([s \in \llbracket u \rrbracket]) + \log(|\llbracket u \rrbracket|^{-1}) - \text{cost}(u)$$

How much more surprising is the data under H_A than H ?

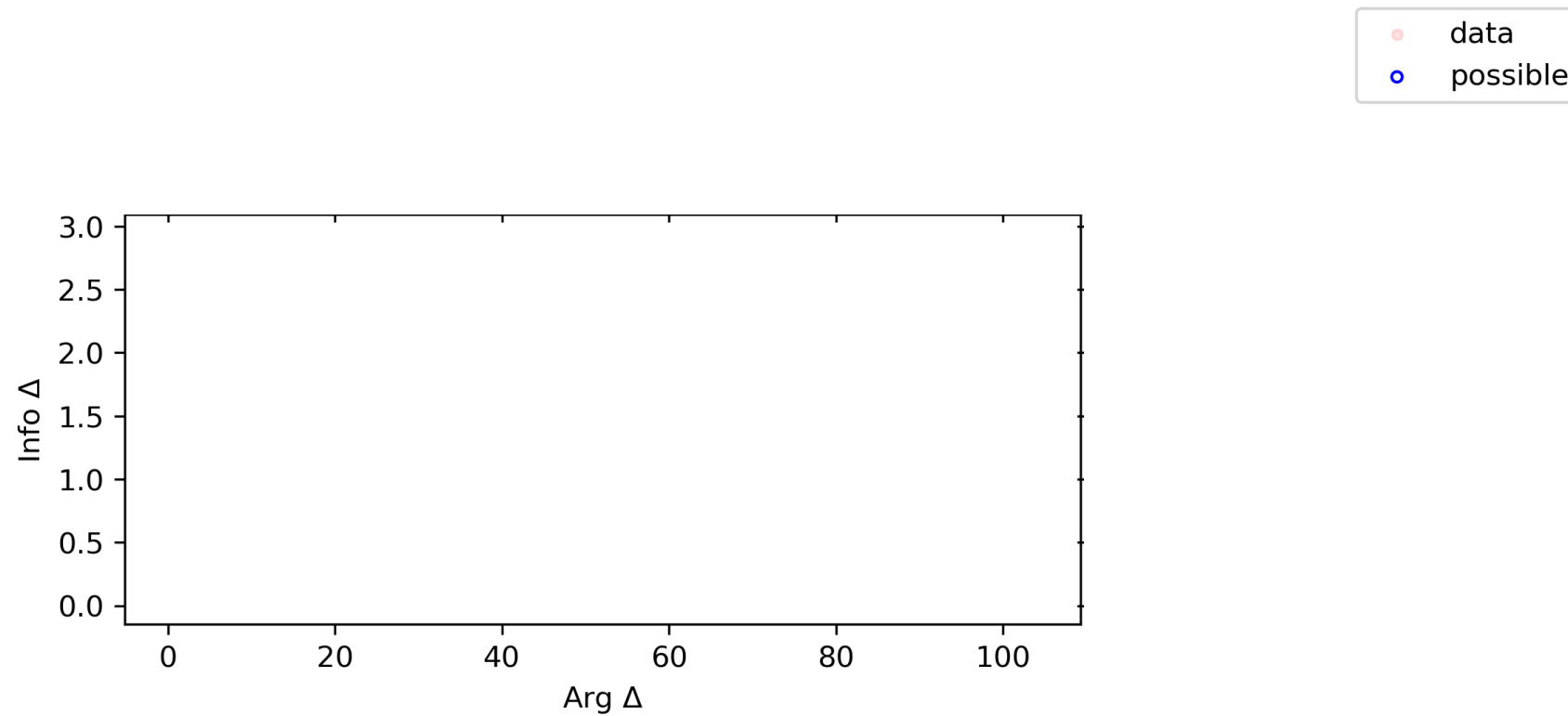
$$\text{argstrength}(u) =$$

$$P_{L_0}(u \mid \gamma) = \sum_o \underbrace{[o \in \llbracket u \rrbracket]}_{\text{Truth}} \underbrace{P(o \mid \gamma)}_{\text{Plausibility of scenario}} \underbrace{|\{u \mid o \in \llbracket u \rrbracket\}|^{-1}}_{\text{Utterance choice}}$$

Quantifying argumentative strength?



Informativity vs. argumentative strength



Basic RSA model

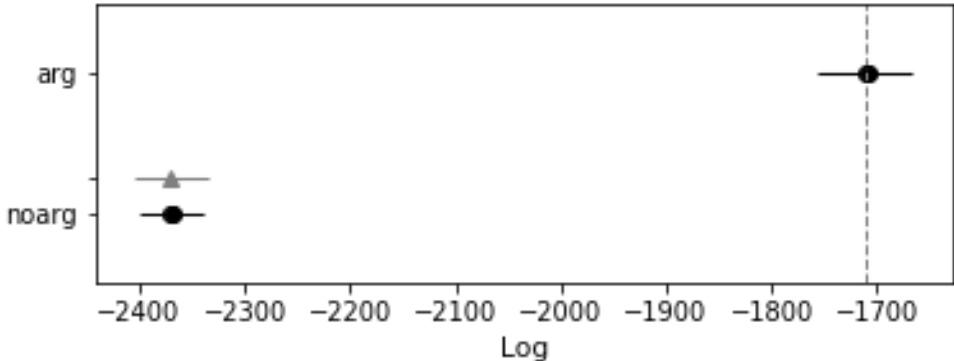
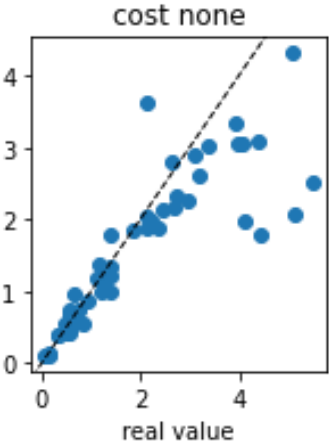
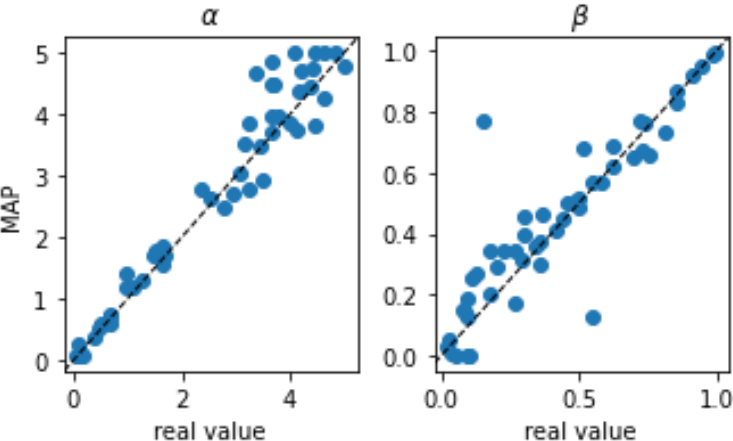
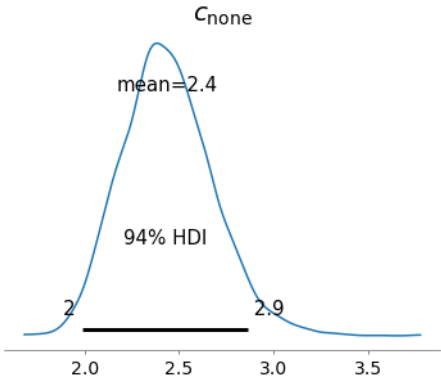
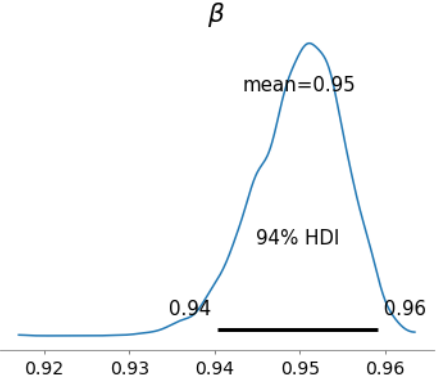
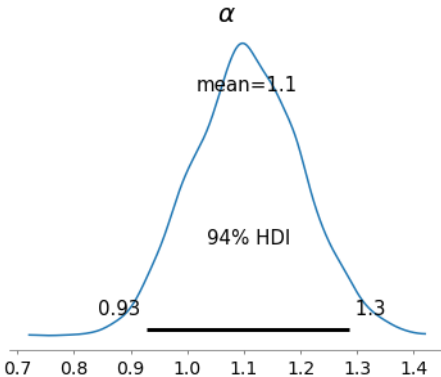
$$\alpha \sim \mathcal{U}(0, 5)$$

$$\beta \sim \mathcal{U}(0, 1)$$

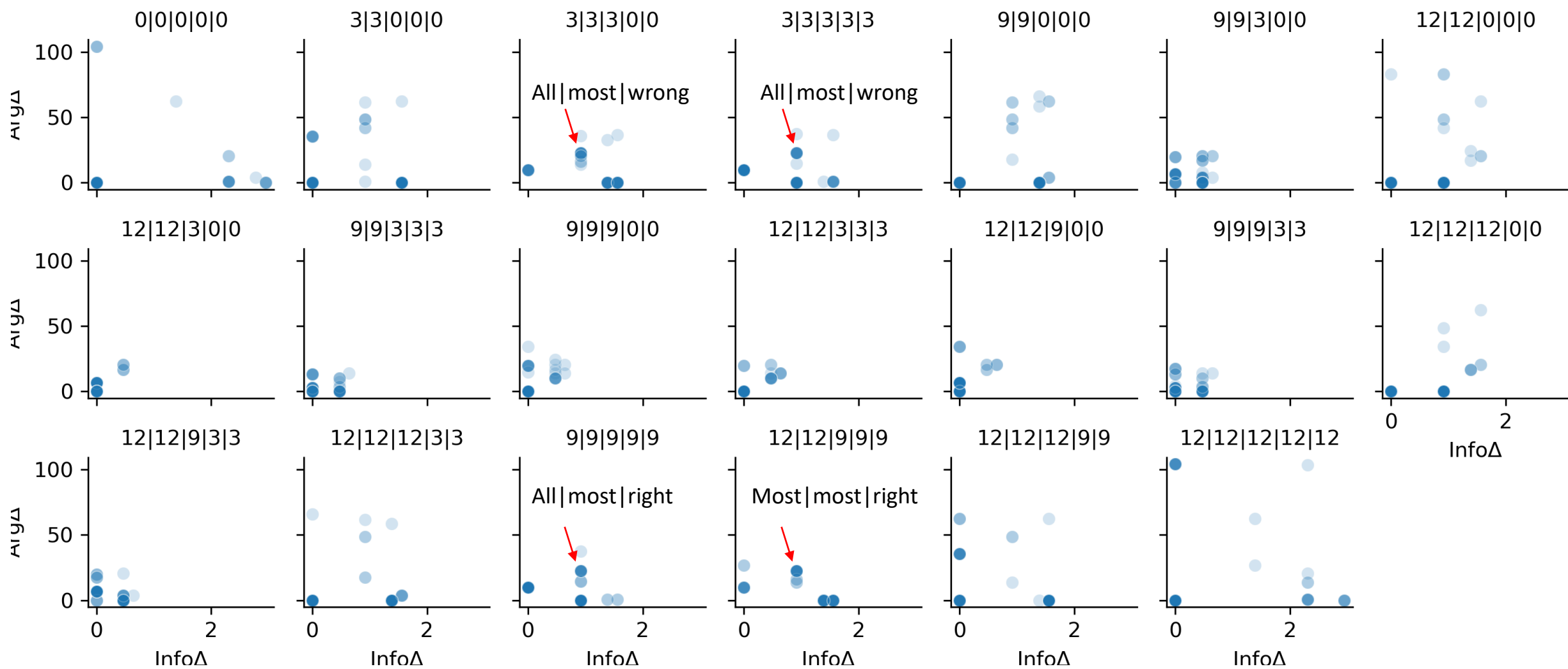
$$c_{\text{None}} \sim \text{Exp}(\lambda = 0.5)$$

$$p_i = \text{RSA}(o_i, \alpha, \beta, c_{\text{None}})$$

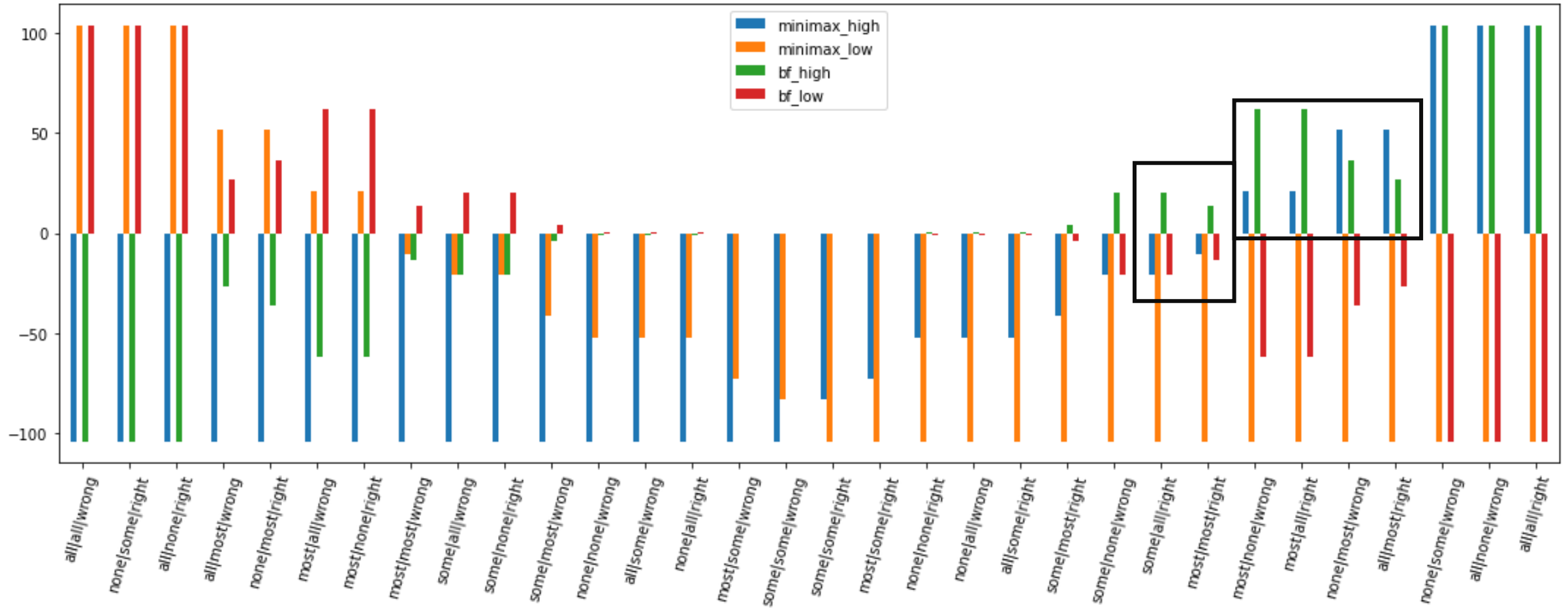
$$u_i \sim \text{Cat}(p_i)$$



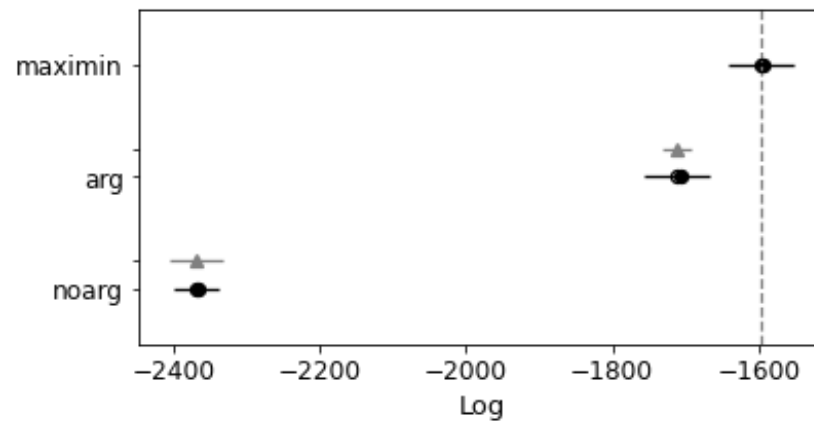
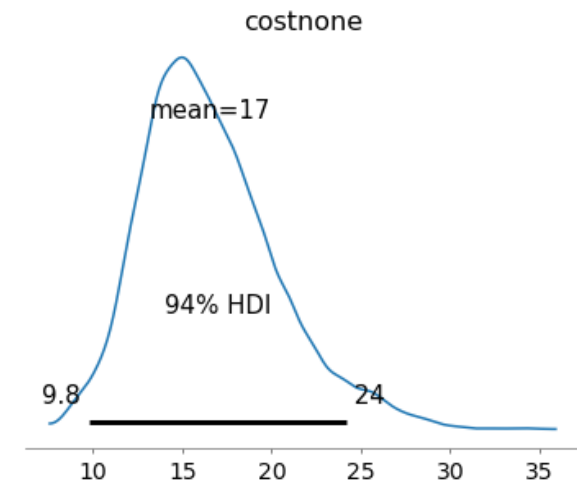
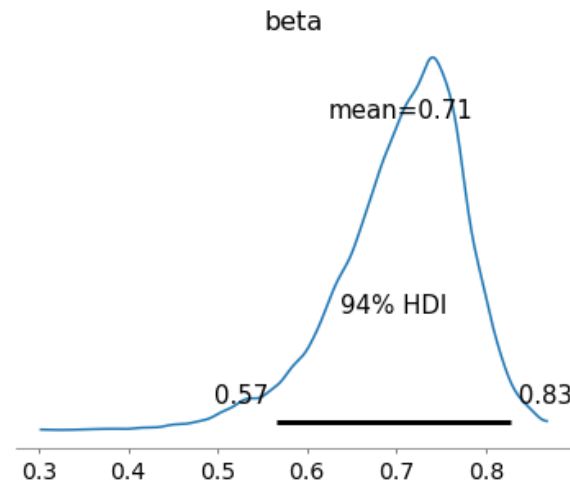
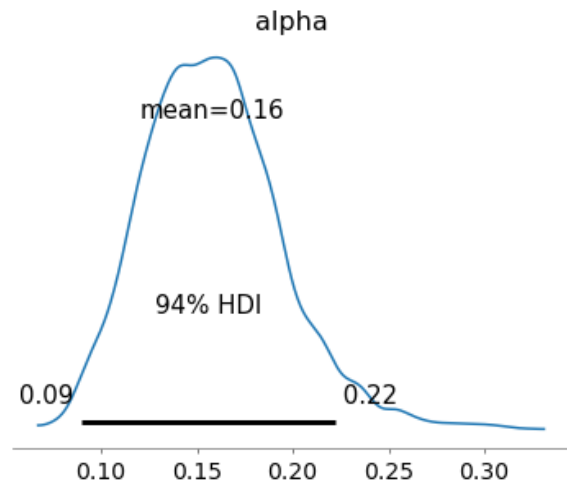
What does the model get wrong?



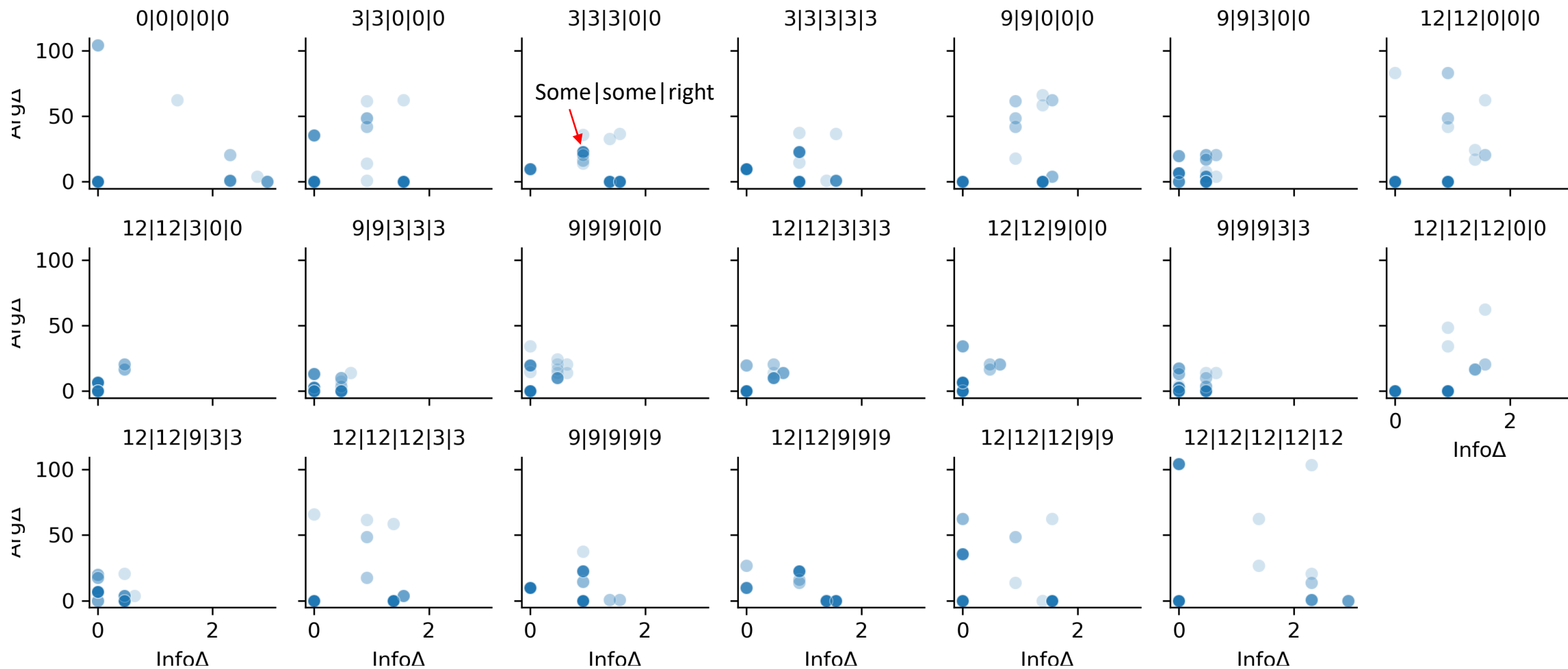
Maximin argstrength



Maximin vs. log lik ratio argstrength



Maximin argstrength



Maximin vs. log lik ratio argstrength

Maximin +

- ‘all|most’ and ‘most|most’ consistently preferred over ‘some|all’.
 - E.g. (12,12,9,0,0), (12,12,9,3,3), (9,9,9,9,9), etc.
- Larger variety of messages for observations that are difficult to argue with
 - E.g. (12,12,12,12,12) in low condition

Maximin -

- ‘Weak’ signals can be bad for both argumentative aims (although possibly best *available*)
- (12,12,12,9,9), high condition: ‘most|all|right’ (predicted by loglikratio) preferred over ‘all|most|right’ (argbest for maximin).

Conclusions

- We have asked participants to choose an utterance while optimizing for a certain argumentative aim.
- Participants were able to do this online.
- We presented an extension of the RSA model that captures much of the participants' behaviour. In this picture we model argumentative strength with log likelihood ratio.
- We have further shown that the basic model systematically fails to predict some pattern.
- We have exploratorily proposed an alternative way of calculating argstrength that predicts the observed pattern.
- Much more work to do!
- Thank you!

Hierarchical RSA model

